

# Calculation Policy 2023-2024

## **CALCULATION POLICY**

Over the years much has changed in the teaching and learning of maths. The calculation methods used by children today in many cases differ from those used by adults when they were at school. This can cause anxiety, with parents and carers unsure whether they should teach children particular methods.

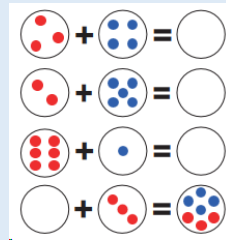
The purpose of this booklet is to provide guidance and information about the types of calculation methods that the children at St. Andrew's are being taught and are using from reception up to Year 2.

This policy lays out the expectations for both mental and written calculations for the 4 number operations and has been created to support the teaching of a mastery approach to mathematics. This is underpinned using models and images that support conceptual understanding and this policy promotes a range of representations to be used across the year groups. Mathematical understanding is developed through the use of representations that are first of all concrete (e.g. Dienes apparatus and place value counters), and then pictorial (e.g. bar models) to facilitate abstract working (e.g. standard written methods). This policy is a guide through an appropriate progression of representations and if at any point a pupil is struggling with the abstract, they should revert to familiar pictorial and/or concrete materials/representations as appropriate.

Although this policy sets out the main methods of mental and written calculations to be taught, it has been appended with a list of recommendations and effective practice teaching ideas aimed at informing and enhancing teaching across all the primary phases. Many of these ideas come from the NCETM's Calculation Guidance document (published October 2015) which is intended to sit alongside a school's calculation policy.



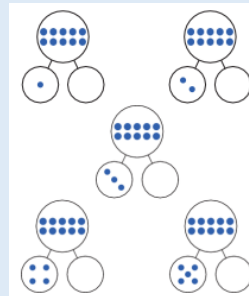
Conceptual Subitising



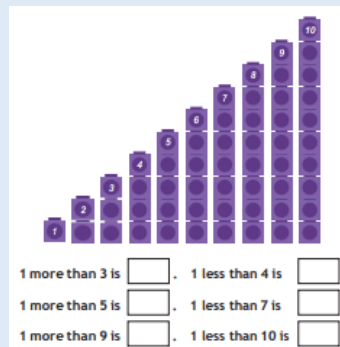
Composition of 5



Composition of 10



Adding 1, 1 More



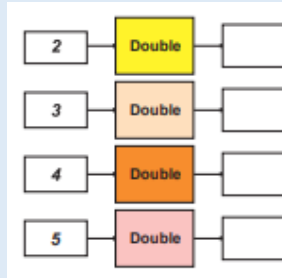
Pupils are able to recognise a quantity by combining groups that have not needed to be counted. Pupils may see 5 items as 3 items and 2 items.

Pupils are able to demonstrate all possible whole number compositions of 5, including recognising and showing 5 on a five frame and using a number bond diagram.

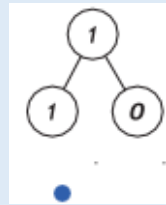
Pupils are able to demonstrate all possible whole number compositions of 10, including recognising and showing 10 on a ten frame and using a number bond diagram.

Pupils relate adding 1 to 1 more than the starting number.

Doubles



Adding zero



Pupils understand doubles up to  $5 + 5$ . This forms the basis of generalising about near doubles. Pupils should also develop an awareness that the sum of any whole number that is doubled will be an even number.

Pupils understand zero can be added to any number but the number will remain unchanged.

Year 1

Part – Part – Whole

+	0	1	2	3	4	5	6	7	8	9	10
0	0+0	0+1	0+2	0+3	0+4	0+5	0+6	0+7	0+8	0+9	0+10
1	1+0	1+1	1+2	1+3	1+4	1+5	1+6	1+7	1+8	1+9	
2	2+0	2+1	2+2	2+3	2+4	2+5	2+6	2+7	2+8		
3	3+0	3+1	3+2	3+3	3+4	3+5	3+6	3+7			
4	4+0	4+1	4+2	4+3	4+4	4+5	4+6				
5	5+0	5+1	5+2	5+3	5+4	5+5					
6	6+0	6+1	6+2	6+3	6+4						
7	7+0	7+1	7+2	7+3							
8	8+0	8+1	8+2								
9	9+0	9+1									
10	10+0										

3 plus 4 EQUALS 7.  
4 plus 3 EQUALS 7.

Pupils develop automatic recall of number bonds to 10. This can be shown using a ten frame, a NUMBER bond diagram and written as an equation. This understanding can be related to adding tens, hundreds and so on when used with a sound understanding of place value.





## Formal Written Method

$43 + 8 = \square$

START by ADDING the ones.

tens	ones
4	3
+	8
1	1

3 ones + 8 ones = 11 ones  
11 ones = 1 ten AND 1 one

RENAME 10 ones AS 1 ten.

tens	ones
4	3
+	8
1	1
+	4
5	1

Then ADD the tens.

4 tens + 1 ten = 5 tens  
 $40 + 10 = 50$

$43 + 8 = 51$

There ARE 51 bottles of water in total.

## Adding Fractions

$\frac{1}{3} + \frac{2}{3}$

$\frac{1}{3} + \frac{1}{3} + \frac{1}{3} = 1$

$\frac{1}{3} + \frac{2}{3}$  make 1 whole.

This is a procedural method that relies on a pupil's conceptual understanding of addition. This begins without renaming and progresses to the renaming of 10 ones into 1 ten. Pupils understand that at this stage, they start with the addition of the ones before they add the tens. This method is supported with base 10 block representation. The formal written method is always accompanied by a written equation to ensure that the relationship between the representations is made.

Pupils use their understanding of adding the same noun when adding fractions through a written sentence. Fractions with the same denominator are added using a '[ ] and [ ] make [ ]' structure.

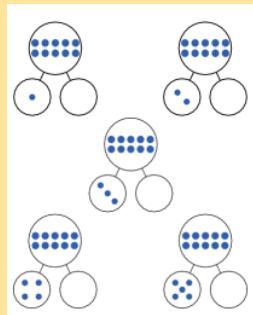




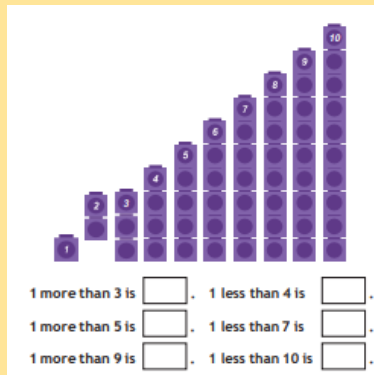
Composition of 5



Composition of 10



Subtracting 1, 1 Less



Doubles

Pupils are able to recognise different quantities by combining within a group without counting them. Pupils can combine these quantities to find the whole amount. This skill is used when subtracting small amounts.

Pupils are able to demonstrate all possible whole number compositions of 5, including recognising and showing 5 on a five frame and using a number bond diagram.

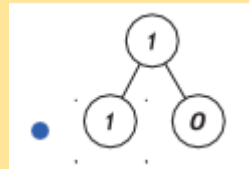
Pupils are able to demonstrate all possible whole number compositions of 10, including recognising and showing 10 on a ten frame and using a number bond diagram.

Pupils relate subtracting 1 to one less than the starting number.

By knowing doubles, pupils can find half of a quantity that remains after half the quantity is subtracted.

Subtracting Zero

10	Half	
8	Half	
2	Half	
6	Half	
4	Half	



Pupils understand zero can be subtracted from any number, but the number will remain unchanged.

Year 1

Part-Part-Whole

This is a mathematical structure that underpins subtraction situations. Numbers can be understood in terms of their parts; understanding that the parts are part of a larger collection. Pupils develop an understanding of the parts and the whole within an equation.

Number Bonds to 10

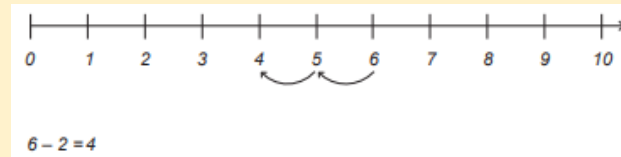
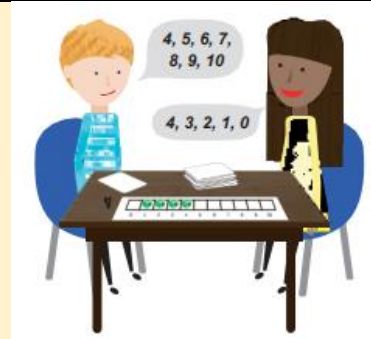
$6 - 2 = \square$

Pupils develop automatic recall of number bonds to 10. This can be shown using a ten frame, a number bond diagram and written as an equation. This understanding can be related to subtracting tens, hundreds and so on when used with a sound understanding of place value.

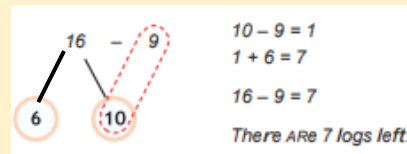
Using a Number Track

Pupils are first introduced to a linear number system through the number

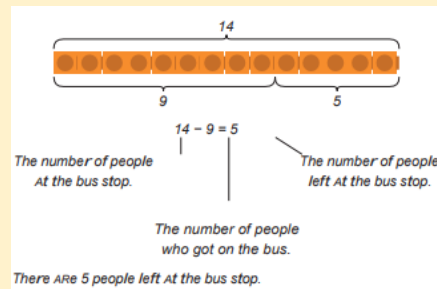
Counting Back Using a Number Line



Subtracting from 10



Subtracting Word Problems



track. This is a precursor to the number line. Pupils may benefit from placing items on the number track as they count and subtract before moving on to use the more abstract number line.

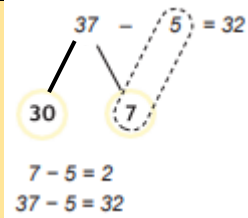
Pupils move from a number track to a number line, starting from zero and having marked increments of 1. The use of the number line is further developed when counting back starts from a given number, relying on pupils' ability to locate and count back from a given number.

Pupils use their part-whole understanding to rename a number into its component parts in order to subtract from 10 within an equation.

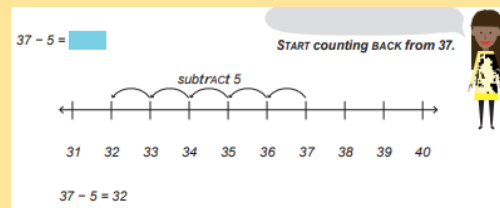
Pupils develop an understanding of situations and problems that require subtraction.

Year 2

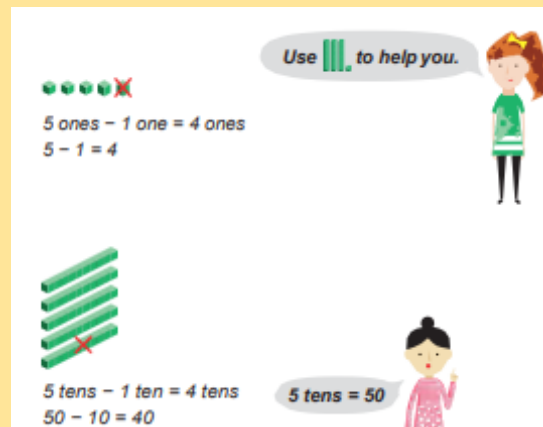
Part-Part-Whole



Counting Back Using a Number Line



Base 10 Blocks

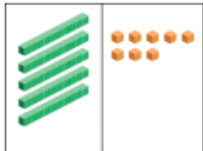


This is a mathematical structure that underpins subtraction situations. Numbers can be understood in terms of their parts; understanding that the parts are part of a larger collection. Pupils develop an understanding of the parts and the whole within an equation.

The use of the number line is further developed when counting back starts from a given number, relying on pupils' ability to locate and count back from a given number, including starting from a 2-digit number. Initially a 1-digit number is subtracted from a 2-digit number, then this progresses to a number line shown with intervals of 10 when subtracting 2-digit numbers that do not have any ones.

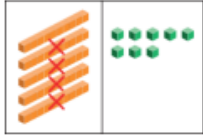
The use of base 10 blocks provides a representation of the place value primarily of 2-digit numbers. This representation is related to the formal written method but also encourages pupils to use their understanding of subtracting the same noun to subtract 2-digit numbers. For example,  $50 - 30$  can

Formal Written Method



8 ones - 0 ones = 8 ones  
8 - 0 = 8

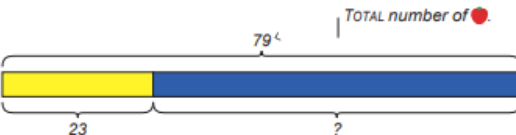
tens	ones
5	8
- 4	0
<hr/>	
	8

5 tens - 4 tens = 1 ten  
50 - 40 = 10  
58 - 40 = 18

tens	ones
5	8
- 4	0
<hr/>	
1	8

Subtraction Word Problems



TOTAL number of 🍓

79


23

?

Number of 🍓 HANNAH AND SAM ATE.

79 - 23 = 56  
There ARE 56 strawberries left.

SUBTRACT 23 from 79.



be understood as 5 tens - 3 tens. The difference between the numbers is 20 or 2 tens. An understanding of place value will support subtraction as well as addition, multiplication and division.

This is a procedural method that relies on a pupil's conceptual understanding of subtraction. Initially, this begins without renaming and progresses to the renaming of 1 ten into 10 ones. Pupils understand that at this stage, they start with the subtraction of the ones before they subtract the tens. This method is supported with base 10 block representation. The formal written method is always accompanied by a written equation to ensure that the relationship between the representations are made.

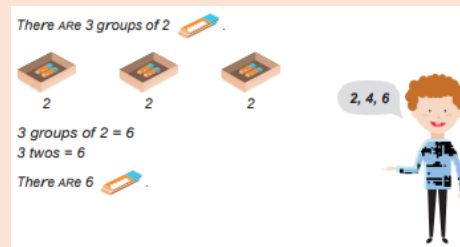
Pupils develop an understanding of situations and problems that require subtraction.



Repeated Addition



Counting in 2s, 5s and 10s



Arrays

diagrams and written numbers. Pupils need to be secure in the abstraction principle of counting the quantity of items, regardless of the properties or characteristics of the items, in order to recognise equal groups in a range of situations.


Initially, multiplication is shown as the addition of equal groups. The key idea of adding like nouns still applies in multiplication. A group of 3 bananas and 3 apples does not result in 6 bananas or 6 apples. In order to add, the nouns must be the same, in this case 6 pieces of fruit. This is also true of multiplication: 2 groups of 3 pieces of fruit makes 6 pieces of fruit.

Pupils start to count in multiples of 2 and multiples of 10, then progress to counting in multiples of 2, 5 and 10 supported by discrete, countable representations.

Multiplication is represented by arrays, beginning with making equal rows and further developing the language associated with arrays. For example: 'There are 3 rows of 5. There are 15 altogether.'



Doubles



1 row of 5 = 5

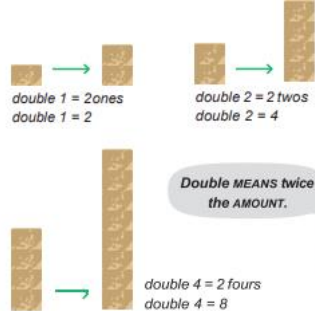
2 rows of 5 = 10

3 rows of 5 = 15

3 fives = 15

There ARE 15 children Altogether.

There ARE 3 rows.



double 1 = 2 ones  
double 1 = 2

double 2 = 2 twos  
double 2 = 4

double 4 = 2 fours  
double 4 = 8

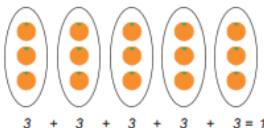
Double MEANS twice the AMOUNT.

JACOB uses 8 blocks next.

The diagrams used to support learning how to double numbers, not only show equal groups of 2 being added each time, but also show the pattern scaling up and each 'tower' being twice the height of the tower just before it. Pupils can develop the language associated with multiplication by describing the growing block pattern. This also provides the basis for understanding halving, in which the representation scales down.

Year 2

Equal Groups



3 + 3 + 3 + 3 + 3 = 15

There ARE 5 groups of 3 ORANGES.

There ARE 15 oranges in total.

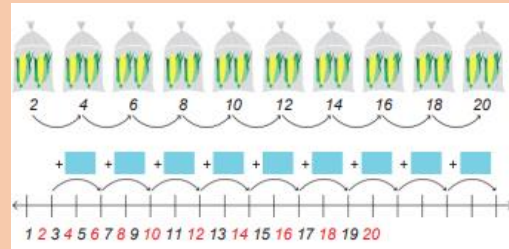
5 threes = 15  
5 groups of 3 = 15  
5 x 3 = 15  
5 times 3 EQUALS 15

We read 5 x 3 = 15 AS 5 times 3 EQUALS 15.

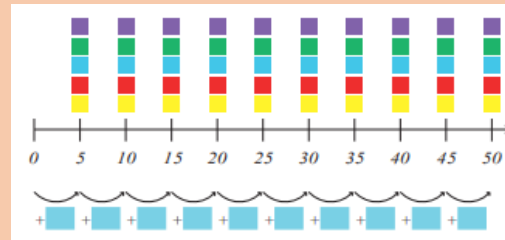
x MEANS to multiply.

Pupils learn to recognise groups that are equal in quantity, initially using like items and then progressing to different items. Pupils understand that equal groups can be represented by concrete items, diagrams and written numbers. In Year 2, the progression to multiplication from repeated addition is shown as 3 + 3 + 3 + 3 + 3 being equal to 5 groups of 3 and 5

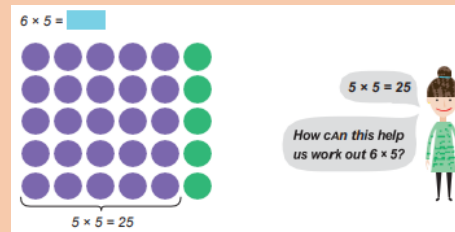
Counting in 2s, 5s and 10s



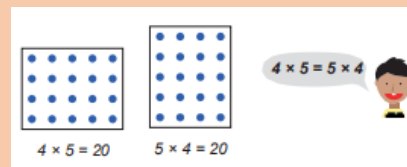
Number Line



Associated Facts



Commutativity



Fact Families

groups of 3 being equal to  $5 \times 3$ . Pupils read  $5 \times 3$  as 5 groups of 3.

When a pupil knows that the size of a group is 2, 5 or 10 and the group size remains consistent, they can count in multiples of 2, 5 and 10 to find the product. Counting in multiples is supported by representation on a number line.

Counting in multiples is shown on a number line. The increasingly abstract nature of the number line is shown as intervals change from 1 to 2, 5 and 10.

As pupils become more fluent and their understanding of their times tables increases, they are expected to use this knowledge to calculate associated facts. A pupil should be able to relate  $10 \times 5$  to  $9 \times 5$ , knowing that the latter expression is 1 group of 5 less. So,  $9 \times 5 = 50 - 5$ .

Pupils learn that the order of the factors in an equation does not affect the product. This is supported pictorially through the use of arrays.

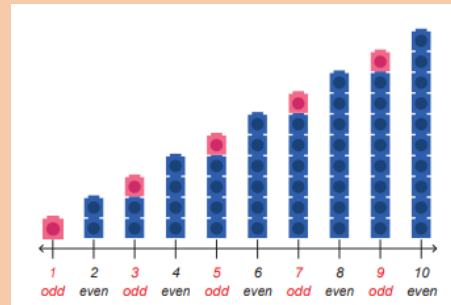
Pupils relate multiplication and division and see the connection

Odd and Even Numbers

$$10 \times 2 = 20 \quad 20 \div 2 = 10$$

$$2 \times 10 = 20 \quad 20 \div 10 = 2$$

There is A  
RELATIONSHIP between  
the MULTIPLICATION AND  
division FACTS.



between them when completing fact families. Pupils develop an understanding that factor  $\times$  factor = product and product  $\div$  factor = factor. Once the understanding of this is secure, pupils can relate this to both multiplication and division situations.

Pupils develop an understanding that even numbers can be put into groups of 2 exactly but when odd numbers are grouped in twos, there is always 1 remaining.

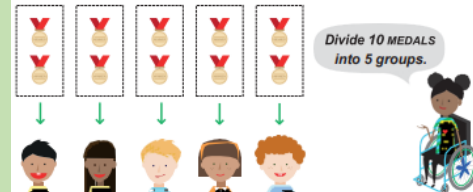
## Division

Year Group	Strand/Topic	Representation	Key Idea
Reception	Equal Groups		<p>Pupils learn to recognise groups that are equal in quantity, initially using like items and then progressing to different items. Pupils understand that equal groups can be represented by concrete items, diagrams and written numbers. Pupils need to be secure in the abstraction principle of counting the quantity of items regardless of the items' properties or characteristics,</p>



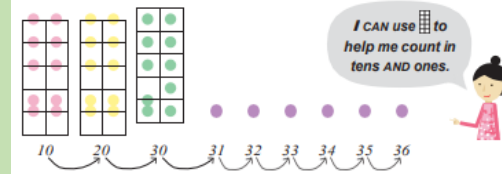
Counting in 2s, 5s and 10s


10 medals ARE SHARED EQUALLY Among 5 friends.  
How many medals does each friend get?



Divide 10 MEDALS into 5 groups.

Each friend gets 2 medals.



I CAN use  to help me count in tens AND ones.

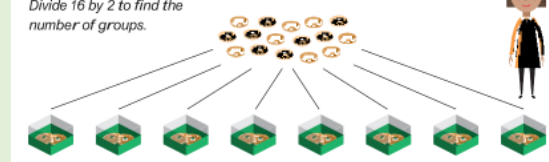
equally between a number of groups. The number of groups is known and pupils find the number of items in each group.

Pupils start to count in multiples of 2 and multiples of 10, then progress to counting in multiples of 2, 5 and 10 supported by discrete, countable representations.

Year 2

Grouping

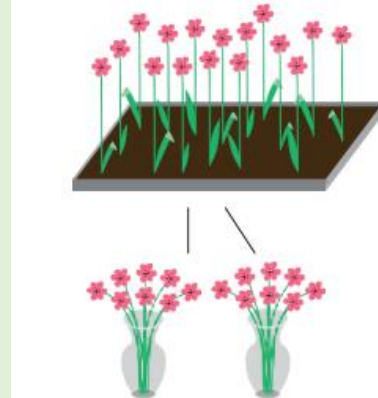
There ARE 16 bagels.  
Divide 16 by 2 to find the number of groups.



I put 2 BAGELS in EACH box.  
There ARE 8 groups of 2.

Sharing

There ARE 16 flowers.  
Elliott cuts the flowers AND puts them equally into 2 vases.



There ARE 8 flowers in each vase.

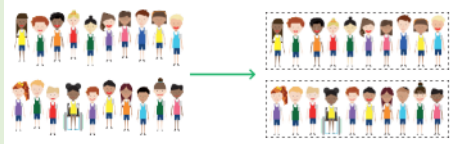
$16 \div 2 = 8$

Pupils initially use grouping for division. They put items into equal groups to find the number of equal groups that can be made from a set amount.

Pupils move from division through grouping to division through sharing. They share a set amount of items equally between a number of groups. The number of groups is known and pupils find the number of items in each group.

Division by 2, 5 and 10

20 children can be put into teams of 10.



$20 \div 10 = 2$   
There ARE 2 equal teams.

There ARE 2 groups of 10 children.


$2 \times 10 = 20$

$10 \times 2 = 20$	$20 \div 2 = 10$
$2 \times 10 = 20$	$20 \div 10 = 2$


There is A RELATIONSHIP between the MULTIPLICATION AND division FACTS.

This is A multiplication And division FACT family.

Odd and Even Numbers



2 cubes can be put into A group of 2.  
4 cubes can be put into groups of 2.  
6 cubes can be put into groups of 2.  
2, 4 And 6 Are even numbers.



1 cube cannot be put into A group of 2.  
3 cubes cannot be put into groups of 2.  
5 cubes cannot be put into groups of 2.  
7 cubes cannot be put into groups of 2.  
1, 3, 5 And 7 Are odd numbers.

Pupils start to make the connection between division and multiplication. They see amounts as equal groups and relate this to multiplication.

Pupils develop an understanding that even numbers can be put into groups of 2 exactly. Numbers that can be put into groups of 2 and have 1 remaining are described as odd numbers.